

# Theoretical investigation of the structural, electronic and thermodynamic properties of cubic and orthorhombic $XZrS_3$ (X = Ba,Sr,Ca) compounds

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#### Abstract

The structural, electronic and thermodynamic properties of XZrS<sub>3</sub> (X = Ba,Sr,Ca) compounds with orthorhombic *Pbnm* and cubic *Pm-3m* phases have been investigated and reported. The calculations have been performed using various density functionals within the generalized gradient approximation. The obtained lattice parameters for the *Pnma* phase reveal very good agreement with experiment. The computed electronic band structures show that in the cubic phase the material of interest is an indirect band-gap (*R*–*T*) semiconductor, whereas it is a direct band gap (*Γ*–*Γ*) in the orthorhombic phase. The semiconducting XZrS<sub>3</sub> (X = Ba,Sr,Ca) compounds are found to satisfy the stability criteria against volume change. Based on the quasi-harmonic Debye model, the thermodynamic properties of the material in question have been predicted taking into account the lattice vibrations. The variation of the lattice constant, bulk modulus, heat capacity, Debye temperature and thermal expansion coefficient as a function of pressure in the range 0–30 GPa and temperatures of 0–1500 K has been computed. Our findings show that external effects such as temperature and pressure are highly effective in tuning some of the macroscopic properties of the compounds under study.

**Keywords** Chalcogenide perovskite  $\cdot$  Phase stability  $\cdot$  Electronic properties  $\cdot$  Thermodynamic properties  $\cdot$  Ab initio calculations

# 1 Introduction

Due to their possible applications in many industrial and engineering domains [1–6], perovskites with different compositions and structures have attracted much attention. These materials have many interesting properties, such as mixed

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conducting oxides for gas separation [7], metallicity and insulating [8], high-temperature electrodes [9], cathode [10], photo-electrode and photo-catalytic [11], photodetector [12], photovoltaic [13], solid electrolyte [14]), hydrogen sensor [15–17], piezoelectric transducer [18], thermostat actuator [19], dielectric resonator [20], magnetic memory and ferromagnetism [21–23], electro-optical modulator [24, 25], laser [26, 27], superconductor [28–30], semiconductivity [31] and ferroelectricity [32, 33].

Recently, perovskite compounds like CeMnO<sub>3</sub>, Rb (Mn,V, Co, Fe)F<sub>3</sub> and BaNpO<sub>3</sub> have been reported to be a half-metallic ferromagnet [34–36]. Similar results were also reported for various other compounds, such as CuMn<sub>2</sub>InSe<sub>4</sub> [37], Li<sub>6</sub>XCl<sub>8</sub> (X = V, Mn, Co and Fe) Suzuki-type compounds [38], (Cr, Mn and V)-doped SrO [39, 40], Sr<sub>2</sub>GdReO<sub>6</sub> double perovskite [41] and quaternary Heusler compound FeCrRuSi [42].

As opposed to their oxide and halide siblings, polycrystalline chalcogenide perovskites ( $BaZrS_3$ ,  $CaZrS_3$  and  $SrZrS_3$ ) have received a little attention. Therefore, only limited data have been published on their physical properties. These materials have proven to be very useful for solar energy conversion applications [43–47]. Their strongly ionic character makes them provide a new avenue for engineering the semiconducting properties for applications, such as energy harvesting, solid-state lighting and sensing.

It should be mentioned that the electronic structure and dielectric constants of BaZrS<sub>3</sub> and CaZrS<sub>3</sub> compounds have been investigated by Sun et al. [48] in three different phases using first-principle calculations. Moreover, Hong et al. [49] have studied the alloy system BaZr<sub>1-x</sub>Ti<sub>x</sub>S<sub>3</sub> suggesting the tunability of the energy band gap. More recently, the electronic band structure of BaZrS<sub>3</sub>, SrZrS<sub>3</sub> and CaZrS<sub>3</sub> in the *Pbnm* phase has been studied by Kuhar et al. [50] using projector augmented wave (PAW) formalism as implemented in the GPAW code [51] and reported band-gap energy values of 2.25, 2.5 and 2.48 eV for BaZrS<sub>3</sub>, SrZrS<sub>3</sub> and CaZrS<sub>3</sub>, respectively.

In Sect. 4 of this paper, the structural, electronic and thermodynamic properties of XZrS<sub>3</sub> are presented. The aim of this work is to examine the electronic band structure of the perovskite XZrS<sub>3</sub>, with emphasis on its derived properties. The calculations are performed with a full relativistic version of the full-potential augmented plane wave (FP–LAPW) and the pseudopotential plane wave (PP–PW) methods within Perdew-Burke-Ernzerhof (PBE)-GGA, Engel-Vosko (EV)–GGA, Hubbard U term GGA + U, Wu and Cohen (WC)-GGA and GGA-Sol as exchange correlation potentials. The remainder of the paper is organized as follows: The theoretical background is described in Sect. 2. Results are presented and discussed in Sect. 3. A summary of the results is given in Sect. 4.

#### 2 Computational methods

In the present work, the experimental crystal structure as reported by Lelieveld and Ijdo [52] has been considered. XZrS3 compounds crystallize in the orthorhombic (space group *Pnma*) structure which is similar to the black structure of  $CsSnI_3$  and cubic symmetry (space group *Pm3m*). The crystal structures of XZrS<sub>3</sub> compound are illustrated in Fig. 1.

The present computations are performed through the FP-LAPW method using DFT as implemented in WIEN2 K code [53]. In the study of structural properties, the exchange correlation energy is treated within the GGA as parameterized by the PBE-GGA method [54]. As a matter of fact, the use of the Engel–Vosko (EV) [55] and Hubbard parameter (GGA + U) [56] approaches so as to treat the exchange–correlation potential is very efficient for studying strongly correlated electrons where the energy band gap of the material of interest can be evaluated more accurately. In these cases, the core electrons are taken to be relativistic, whereas the

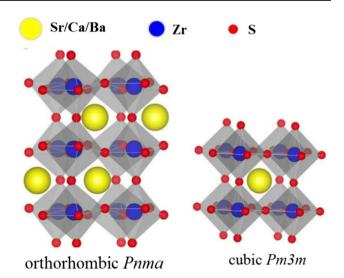


Fig. 1 Crystal structure of orthorhombic *Pbnm* and cubic *Pm-3m* phases of XZrS<sub>3</sub> compounds

valence electrons are considered to be as semi-relativistic. This is probably best suited for our system and for a fullpotential method. The threshold energy between valence and core states is set to be -6.0 Ry. Here, the Kohn-Sham equations are solved by expanding the wave functions in the spherical harmonics form inside the atom spheres. A plane wave expansion has been used in the interstitial regions of atoms inside the unit cell. We have used lmax = 10 for angular momentum expansion and  $R_{\rm MT}K_{\rm max} = 8$  as a plane wave cutoff with 500 and 3000 k points for orthorhombic and cubic phases, respectively. Here,  $R_{\rm MT}$  is the average muffintin (MT) radius and K<sub>max</sub> is the wave function cutoff. The radii  $R_{\rm MT}$  of the muffin tins (MT) are chosen to be approximately proportional to the corresponding ionic radii. The energy between successive iterations is converged to 0.0001 Ry, and forces are minimized to  $1 \text{ mRy Bohr}^{-1}$ .

We have also used the ultra-soft pseudo-potentials of the Vanderbilt-type [57], and the GGA approach according to PBE [54], GGA-Sol [58] and GGA-WC [59] was already used to calculate structural and electronic properties of XZrS<sub>3</sub>. A computer program CASTEP (Cambridge Serial Total Energy Package) [60] was already used to calculate structural and electronic properties of XZrS<sub>3</sub>. The kinetic cutoff energy for the plane wave expansion is taken to be 500 eV for all cases being considered here. The special k point sampling for the integration of first Brillouin zone has been employed by using the Monkhorst-Pack method with  $10 \times 10 \times 10$  k points for a cubic phase and  $7 \times 7 \times 7$  k points for the orthorhombic phase. Based on the Broyden-Fletcher-Goldfarb-Shanno (BFGS) [61] minimization technique, the system reached the ground state via self-consistent calculation when the total energy is stable to within  $5 \times 10^{-6}$  eV atom<sup>-1</sup> the force is less than  $10^{-2}$  eV Å<sup>-1</sup>.

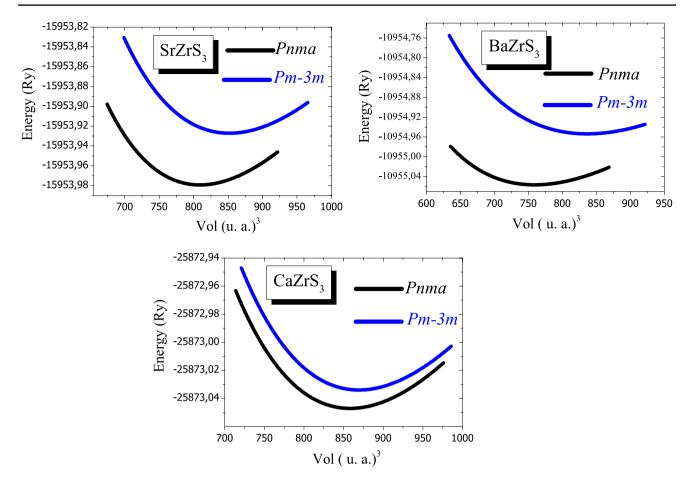


Fig. 2 Calculated normalized energy as a function of volume for XZrS<sub>3</sub> compound

To investigate the thermodynamic properties of  $XZrS_3$  compounds, the quasi-harmonic Debye model [62] has been applied. In this model, the non-equilibrium Gibbs function  $G^*(V;P,T)$  is expressed as follows:

$$G^*(V;P,T) = E(V) + PV + AVib[\theta(V);T]$$
(1)

where E(V) is the total energy per unit cell, *PV* corresponds to the constant hydrostatic pressure condition,  $\theta(V)$  is the Debye temperature and *Avib* is a vibrational term that can be written using the Debye model of the phonon density of states as [63],

$$A_{\rm vib}(\theta;T) = nkT \left[\frac{9\theta}{8T} + 3\ln(1 - e^{-\theta/T}) - D(\theta/T)\right]$$
(2)

where *n* is the number of atoms per formula unit and  $D(\theta/T)$  is the Debye integral. For an isotropic solid,  $\theta$  is given as [64],

$$\theta_D = \hbar \left[ 6\pi^2 V^{1/2} n \right]^{1/3} f(\rho) \sqrt{\frac{B_S}{Mk_B^2}}$$
(3)

where M is the molecular mass per unit cell and  $B_S$  is the adiabatic bulk modulus. The latter is approximated by the static compressibility [63] as

$$B_S \cong B(V) = V \frac{d^2 E(V)}{dV^2} \tag{4}$$

 $f(\rho)$  in Eq. (3) is reported in Refs. [64, 65]. The Poisson ratio  $\nu$  is taken to be 0.25 [66]. Thus, the non-equilibrium Gibbs function  $G^*(V;P,T)$  versus (V; P, T) is minimized with respect to the volume V as

$$\left[\frac{\partial G^*(V;P,T)}{\partial V}\right]_{P,T} = 0$$
(5)

By solving Eq. (5), one can obtain the thermal equation of state (EOS) V(P,T). The heat capacity  $C_V$  and the thermal expansion coefficient  $\alpha$  are given by [67, 68],

$$C_V = 3nk \left[ 4D\left(\frac{\theta}{T}\right) - \frac{3\theta/T}{e^{\theta/T} - 1} \right]$$
(6)

<b>Table 1</b> Lattice constant $a$ (Å), $b$ (Å), $c$ (Å), bulk modulus $B$ (in GPa) and first pressure derivative of bulk modulus $B'$ for XZrS <sub>3</sub>	Compound		а	b	С	V <sub>0</sub>	В	<i>B'</i>
	BaZrS <sub>3</sub>							
	Pnma	FP-LAPW	7.0598	9.9813	7.0250	495.0235	73.2240	4.1562
		PP-PW	7.1753	10.0570	7.0534	508.9873	123.4053	_
		Exp [52]	7.0599	9.9813	7.0251	495.04	_	_
		[70]	7.04	9.98	7.05	_	_	_
		Other [77]	7.054	7.155	10.068	_	_	_
		[77]	7.112	7.299	10.181	_	_	_
		[78]	7.06	7.16	10.04	_	_	_
		[78]	7.03	7.12	10.00	_	_	_
	Pm-3m	FP-LAPW	5.0504	_	_	126,5060	72.5519	4.1477
		PP-PW	5.0211	_	_	128.3901	69.3380	
		Exp [70]	4.192	_	_	_	_	_
		Other [78]	4.195	_	_	_	_	_
		[73]	4.242	_	_	_	_	_
		[75]	4.198	_	_	_	_	_
		[77]	4.234	_	_	_	_	_
		[77]	4.207	_	_	_	150	_
	CaZrS <sub>3</sub>							
	Pnma	FP-LAPW	7.0856	9.6647	6.5588	449.1479	82.4513	4.1716
		PP-PW	7.0719	9.6611	6.5817	449.6771	105.7320	_
		Exp [52]	7.0300	9.5896	6.5366	440.66		
	Pm-3m	FP-LAPW	4.9859	_	_	123.9455	75.3506	3.7145
		PP-PW	4.9801	_	_	123,5059	74.4015	
		Exp [79]	4.020	-	-	_	_	_
		Exp [81]	4.138		_	_	_	_
		Other [82]	4.064	177.7	_	_	_	_
	SrZrS <sub>3</sub>							
	Pnma	FP-LAPW	7.1474	9.8425	6.8046	478.6919	77.3524	4.1462
		PP-PW	7.1692	9.8362	6.7839	478.3849	101.9356	_
		Exp [52]	7.1085	9.7661	6.7350	467.56	_	_
		Other [78]	6.79	7.16	9.84	_	-	-
		[78]	6.75	7.13	9.79	_	_	_
	Pm-3m	FP-LAPW	5.0163	-	-	126,2265	73.4956	3.9978
		PP-PW	5.0085	-	_	125.6385	71.1959	

$$S = nk \left[ 4D\left(\frac{\theta}{T}\right) - 3\ln(1 - e^{-\theta/T}) \right]$$
<sup>(7)</sup>

$$\alpha = \frac{\gamma C_V}{B_T V} \tag{8}$$

where  $\gamma$  is the Grűneisen parameter, which is defined as

$$\gamma = -\frac{\mathrm{d}\ln\theta(V)}{\mathrm{d}\ln V} \tag{9}$$

Through the quasi-harmonic Debye model, one could calculate the thermodynamic quantities at any given temperatures and pressures of XZrS3 compounds from the obtained E–V data at T=0 and P=0.

# **3** Results and discussion

The total energy has been obtained versus the unit-cell volume  $V_0$  for both orthorhombic (*Pnma*) and cubic (*Pm-3m*) phases of the material system of interest. Our results are displayed in Fig. 2 and fit to the Murnaghan equation of state [69]. This allowed the determination of the equilibrium lattice constants a (Å), b (Å) and c (Å) and bulk modulus B (GPa) and its first pressure derivative B'. The resulting structural parameters for both phases being considered in the present work are listed in Table 1. Also shown for comparison are the available experimental and theoretical data quoted in the literature. A good accord can be observed between our findings and the experimental [52, 70, 71, 79, 80] and previous theoretical data [72–78, 81] regarding a

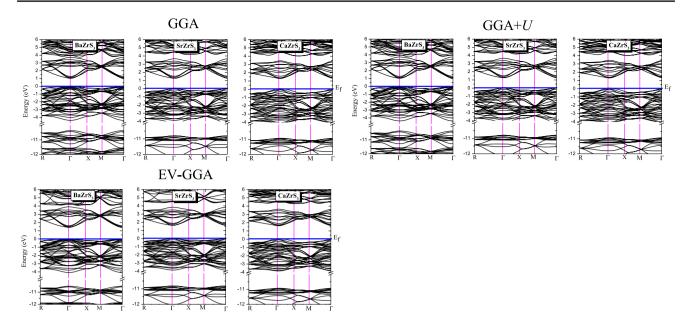


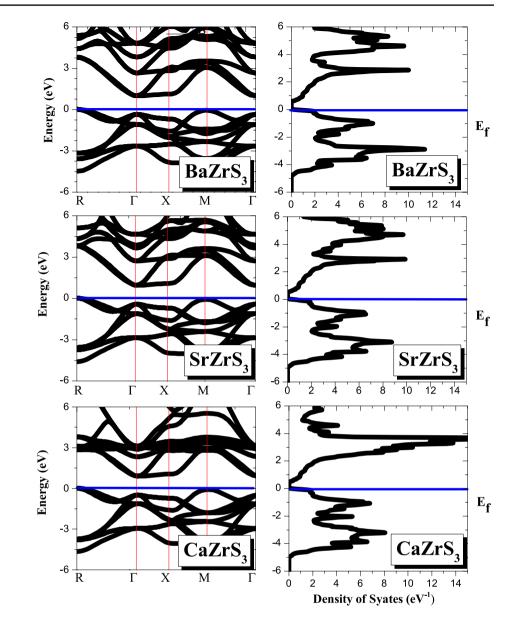
Fig. 3 Band structure for high-symmetry directions in the Brillouin zone of orthorhombic Pbnm structure

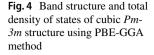
(Å), b (Å) and c (Å) lattice parameters. Our results indicate that the *Pnma* phase of XZrS<sub>3</sub> is at its ground state. It can also be seen that  $V_0$  for both orthorhombic (*Pnma*) and cubic (Pm-3m) phases has an increasing trend along the sequence  $Ca \rightarrow Sr \rightarrow Ba$ . The increase in  $V_0$  for X = Ca, Sr and Ba successively satisfies the increasing order of the X atomic radii, namely r(Ca = 1.64 Å) < r(Sr = 1.72 Å) < r(Ba = 1.88 Å [82]. The behavior seems to be similar to that of RbMF<sub>3</sub> (M=Be, Mg, Ca, Sr and Ba) compounds [83]. As shown in Table 1, our results regarding the bulk modulus B of BaZrS<sub>3</sub> in the cubic (Pm-3m) phase yielded a value of 72.55 GPa when using FP-LAPW method and a value of 69.34 GPa when using PP-PW method. As compared to the value of B = 150 GPa reported by Bilić and Gale [76], our results seem to be much smaller than those of Ref. [76]. The disagreement between our results and those of Bilić and Gale [76] may be attributed to the neglect of the barium  $5s^2$  and  $5p^6$  electrons in the valence configuration of Ba. B is a measure of the material crystal rigidity. Thus, as far as the value of B is large, the material becomes more rigid. In our case, B increases in the following order:  $B(KAlO_3) > B($  $RbAlO_3$  >  $B(CsAlO_3)$ . The increasing trend reveals that the rigidity and the hardness of the material in question increase in the same sequence.

Figures 3 and 4 show, respectively, the self-consistent scalar relativistic band structures and density of states of  $XZrS_3$  in its both orthorhombic and cubic phases. The band structure and density of states computed via the FP–LAPW approach are shown as a prototype given the fact that the band profiles obtained from FP–LAPW

approach are quite similar to those calculated via PP-PW method with a negligible difference in details. Based on the lattice symmetry, the integration paths  $R-\Gamma-X-M-\Gamma$ are performed so as to treat the band structure for both phases of interest, i.e., orthorhombic and cubic phases. For the orthorhombic phase, both the valence band maximum (VBM) and the conduction band minimum (CBM) occur at the high-symmetry point  $\Gamma$  in the Brillouin zone. Hence, in this phase the material being studied here is a direct bandgap semiconductor. However, as far as the cubic phase is concerned, the VBM occurs at R point and the CBM is located at the  $\Gamma$  point. Therefore, the material in question is an indirect band-gap semiconductor in its cubic phase. The computed energy band gaps given in Table 2 for the orthorhombic phases seem to be underestimated with respect to the experimental ones of 1.8 [76, 80], 2.13 [76] and 1.9 eV [76] reported for BaZrS<sub>3</sub>, SrZrS<sub>3</sub> and CaZrS<sub>3</sub>, respectively. The previous computational studies appear to give much larger values than those found in the present work for most cases of interest. It is worth noting that the computed energy band gaps of all compounds being studied here are calculated better (as compared to experiment) when using the GGA-EV approximation. The disagreement of our results with respect to experiment is due to the use of GGA approach which is well known to underestimate the energy band gaps with respect to experiment.

The nature of the electronic band structure has been elucidated by calculating the total and partial densities of states (DOS) of  $BaZrS_3$ ,  $SrZrS_3$  and  $CaZrS_3$  compounds in the energy range – 12 to 6 eV (see Fig. 5). By observing Fig. 5,





one can note that the overall features of the DOS for all compounds of interest are similar. At low energies and in particular in the core states the main contribution is due to the hybridization of X-p and S-s states. Nevertheless, the valence bands are considered in the energy range from -4 to 0.0 eV. In the valence band, mixed S-p and X-p states are prominent. The conduction band is above the Fermi level. This band is essentially composed of X-s and Zr-d states. Meanwhile, the electronic structure has also been computed versus pressure and is plotted in Fig. 6. We observe a clear shift of the Fermi level. Nevertheless, one can note a preserved semiconducting nature for both band structures of interest in the stress range of 0% up to 14%.

The thermodynamic properties of the compounds of interest have also been investigated under high pressure and at high temperatures. For that, we have applied the quasi-harmonic Debye approximation. We start first by calculating a set of total energy as a function of the primitive cell volume (E-V) in the static approximation. Then, the obtained data are fit with a numerical EOS so as to obtain the structural parameters at pressure and temperature of zero, and to derive the macroscopic properties versus pressure and temperature using standard thermodynamic relations.

The diagrams that represent the volume unit-cell temperature at various pressures and lattice constant pressure Table 2Calculated energyband gap for orthorhombic andcubic phases using GGA-PBE,GGA-EV, GGA-WC, GGA-Soland GGA + U approaches

Compounds	This work (FP-LAPW)			This work (	PP-PW)	Exp	Others	
	GGA-PBE	GGA-EV	GGA + U	GGA-PBE	GGA-Sol	GGA-WC		
BaZrS <sub>3</sub>								
(Pnma)	1.051	1.424	1.063	1.202	1.109	1.117	1.8 [70] 1.8 [76]	1.02 [78] 1.82 [79] 1.7 [80] 2.34 [81] 2.25 [82]
(Pm-3m) CaZrS <sub>3</sub>	0.553	0.996	0.548	0.554	0.425	0.545	-	-
(Pnma)	1.311	1.637	1.362	1.303	1.177	1.185	1.90 [70]	2.48 [ <b>78</b> ] 2.48 [ <b>82</b> ]
( <i>Pm-3m</i> ) SrZrS <sub>3</sub>	0.446	0.899	0.469	0.424	0.288	0.325		
(Pnma)	1.268	1.617	1.288	1.280	1.151	1.160	2.13 [70]	2.04 [76] 2.50 [79] 2.50 [82]
( <i>Pm-3m</i> )	0.492	0.975	0.492	0.492	0.383	0.400	_	_

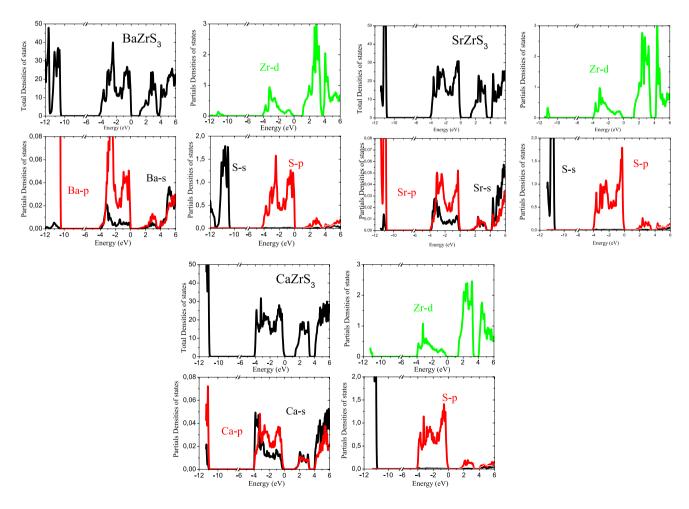


Fig. 5 Total and projected density of states of Pbnm structure using PBE-GGA method

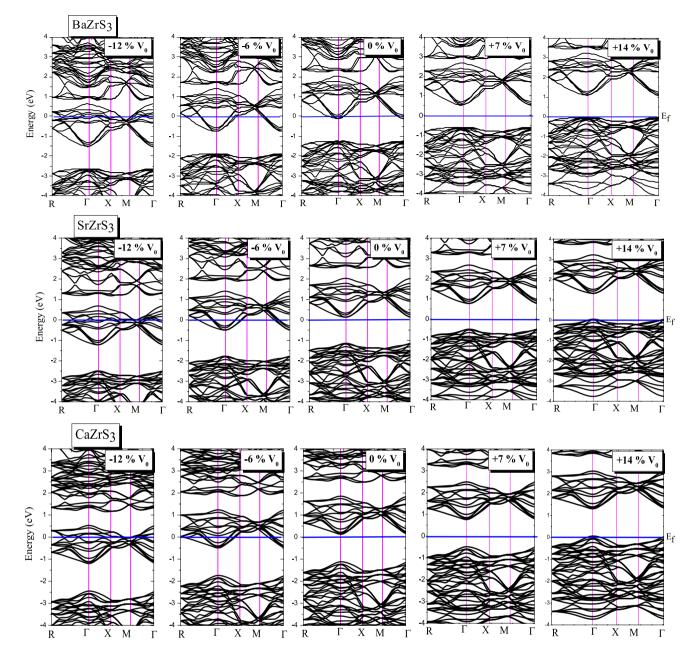


Fig. 6 Calculated band structure of Pbnm structure using PBE-GGA method: pressure effect

at different temperatures for all compounds being studied here are shown in Fig. 7. Note that for a given pressure, the lattice constant increases monotonically with rising temperature. Nevertheless, the rate of increase seems to be very moderate. On the other hand, for a given temperature, the lattice constant decreases with increasing pressure. In the present work, our calculated volumes for BaZrS<sub>3</sub>, SrZrS<sub>3</sub> and CaZrS<sub>3</sub> compounds at zero pressure and room temperature are found to be 509.31, 480.13 and 453.47  $\text{\AA}^3$ , respectively.

The variation of the bulk modulus as a function of temperature at different pressures ranging from 0 to 30 GPa is plotted in Fig. 8. We observe that the bulk modulus varies

almost linearly versus temperature for all pressures of interest. It decreases monotonically and very slowly with the rising temperature. Our calculations of the bulk modulus at a temperature of 300 K and zero pressure yielded values of 292.33, 308.86 and 329.16 GPa for BaZrS<sub>3</sub>, SrZrS<sub>3</sub> and CaZrS<sub>3</sub> compounds, respectively.

The evolution of the heat capacity at a constant volume C<sub>v</sub> as a function of temperature at various pressures ranging from 0 to 30 GPa is displayed in Fig. 9. Note that C<sub>v</sub> increases with rising temperature. The behavior appears to be rapid at low temperatures but becomes slow at high temperatures. For temperatures less than 900 K, C<sub>V</sub>

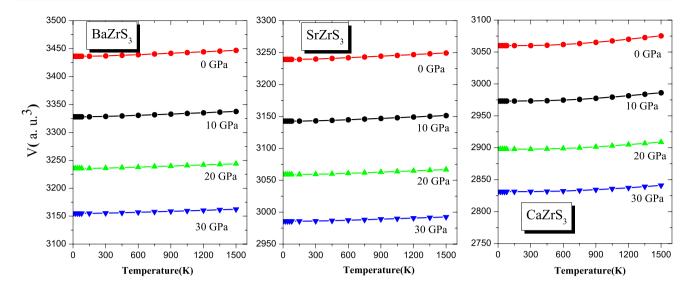


Fig. 7 Temperature dependence of the volume at various pressures for XZrS<sub>3</sub> compounds

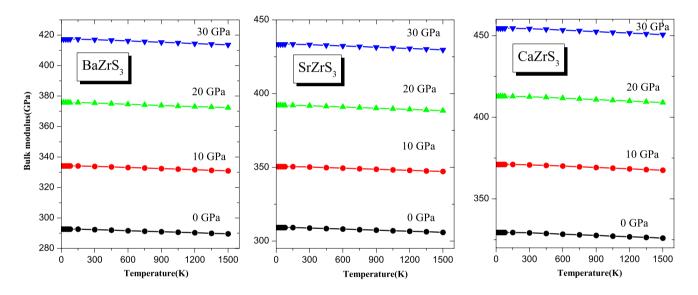


Fig. 8 Temperature dependence of the Bulk modulus B at various pressures for XZrS<sub>3</sub> compounds

depends on both temperature and pressure. At high temperatures,  $C_V$  approaches approximately 121.94, 120.92 and 120.17 J mol<sup>-1</sup> K<sup>-1</sup> for BaZrS<sub>3</sub>, SrZrS<sub>3</sub> and CaZrS<sub>3</sub> compounds, respectively. The details in this change seem to depend on pressure. The behavior of  $C_V$  for all compounds of interest exhibits similar features in a wide range of pressures and temperatures. At zero pressure and a temperature of 300 K, our findings yielded values of  $C_V$  of about 81.98, 75.38 and 61.98 J mol<sup>-1</sup> K<sup>-1</sup> for BaZrS<sub>3</sub>, SrZrS<sub>3</sub> and CaZrS<sub>3</sub> compounds, respectively. In order to reflect the temperature dependence of the volume, the Debye temperature is calculated using the quasi-harmonic Debye approximation. Our results are shown in Fig. 10. Note that the Debye temperature of all compounds in question increases with rising temperature. It is worth noting that the Debye temperature decreases with increasing the atomic number of X (X = Ba, Sr and Ca). The temperature dependence of the thermal expansion coefficient  $\alpha$  of the (Ca, Sr, Ba)ZrS<sub>3</sub> compounds at various pressures is depicted in Fig. 11; it is clear that below 600 K, the thermal expansion coefficient increases rapidly, whereas at temperatures higher than 600 K, the  $\alpha$  value initially remains constant and then increases linearly at high pressure. At zero pressure and T = 300 K,  $\alpha$  takes the values of  $0.16 \times 10^{-5} \text{K}^{-1}$ ,  $0.13 \times 10^{-5} \text{K}^{-1}$  and  $0.17 \times 10^{-5} \text{K}^{-1}$  for CaZrS<sub>3</sub>, SrZrS<sub>3</sub> and BaZrS<sub>3</sub>, respectively.

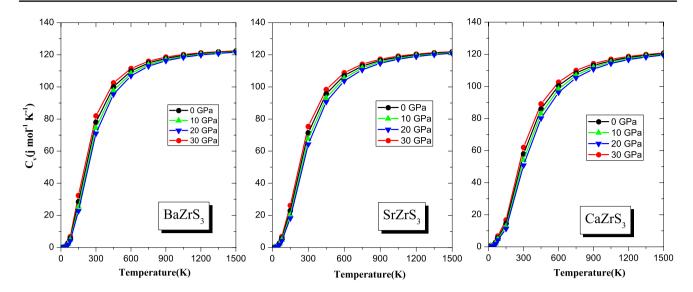


Fig. 9 Variation of the heat capacities Cv versus temperature at various pressures for XZrS<sub>3</sub> compounds

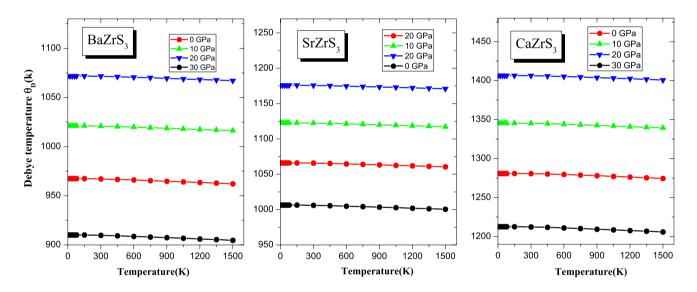


Fig. 10 Variation of the Debye temperature  $\theta_D$  as function of temperature at various pressures for XZrS<sub>3</sub> compounds

### 4 Conclusion

In conclusion, the electronic and structural properties of cubic and orthorhombic  $XZrS_3(X = Ba, Sr, Ca)$  were investigated using both PP-PW and FP-LAPW methods. The computed lattice parameters, namely *a*, b and *c*, and the bulk modulus and its first pressure derivative were found to be in good accord with data available in the literature. Our results regarding the electronic band structures showed that

the transition in the cubic phase occurs along R- $\Gamma$  in the first Brillouin zone indicating thus that the material of interest is an indirect band-gap semiconductor in this phase. However, the transition in the orthorhombic phase was found to occur along  $\Gamma$ - $\Gamma$  in the first Brillouin zone suggesting that the material of interest is a direct band-gap semiconductor in that phase. The semiconducting materials XZrS<sub>3</sub> of interest were found to be stable against volume change of 0 to + 14%. The thermal and pressure effects on the macroscopic

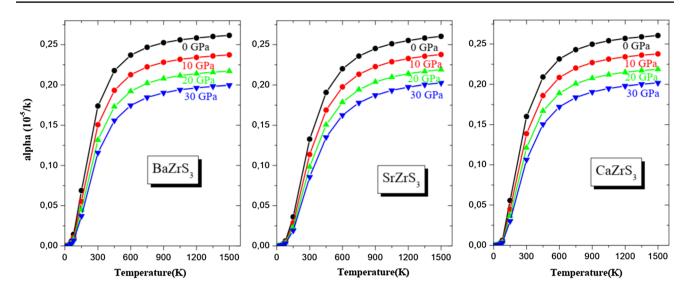


Fig. 11 Variation of the thermal expansion coefficient  $\alpha$  of the XZrS3 compounds versus temperature at several pressures

properties of the compounds under study were predicted using the quasi-harmonic Debye model where the lattice vibrations were taken into consideration. The behavior of the lattice constant, bulk modulus, heat capacity, Debye temperature and thermal expansion coefficient as a function of both temperature and pressure was examined.

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