# Three Level Four Leg Shunt Active Power Filter Based a New Three Dimensional Space Vector Modulation strategy in the αβ0-axes

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*Abstract*—This paper presents a new Three level Three Dimensional Space Vector Modulation (Three level 3D-SVM) strategy for three level four leg Neutral Point Clamped (NPC) inverter controlling which is competent to operate in Shunt Active Power Filter (SAPF), in order to reducing the source harmonic currents and the inverter harmonic output voltages, eliminating the zero-sequence current caused by single-phase non-linear loads, reducing the switching frequency and voltage supported by the switches, and to compensate the reactive power. Simulation results of three level four leg Shunt Active Power Filter performances are presented to validate the proposed three level 3D-SVM strategy for switching signals generating.

Keywords—Three level four leg SAPF, Three Level Three Dimensional Space Vector Modulation (Three-Level 3D-SVM), pq0 Theory; Zero-sequence current; Harmonic currents compensation; Reactive power compensation, PI.

#### I. INTRODUCTION

The four leg shunt active power filters (SAPFs) have extensively studied and effectively solution for improve the largely power factor by the compensation of harmonic currents , reactive power and zero sequence current elimination in three phase four wire electrical networks caused by three singlephase non-linear loads [1-3]. The four leg shunt active power filters commonly based on an four leg inverter for injects harmonics and zero sequence current in the electrical network, equal to that given by single phase non-linear loads, but in phase opposition there with into the point of common coupling (PCC) [4,5]. The four leg shunt active power filters are individual widely used on gained large of their capability to compensate for harmonics, zero sequence current and reactive power simultaneously in four wire network [5–7].

Conventional two-level four leg inverter configurations used as shunt active power filters are simply appropriate for low to medium power applications. However, multilevel inverter configurations are appropriate for high voltage, and medium to high power applications [8]. Three level three or four leg Neutral Point Clamped (NPC) inverters are now suitable exceptionally accepted for high power applications such as static var compensation, motor drives, and active Mohamed F. Benkhoris IREENA Laboratory University of Nantes at Saint Nazaire France Mohamed-Fouad.Benkhoris@univnantes.fr Abdelhalim Kessal Faculty of Science and Technology University of Bordj Bou Arreridj Algeria abdelhalim.kessal@yahoo.fr

power filters [9–14], due to their advantages over the conventional two level inverters as they result in high voltage capability, almost sinusoidal output voltage and power quality associated with reduced harmonic distortion, lower electromagnetic interference (EMI) [22]. They can increase output voltage magnitude and reduce output voltage harmonic, switching frequency and voltage supported by each switch, and elevated competence than two level four leg inverter for active power filters and high power compensation applications [11]. Also the output voltage forms and the switching losses depends on the technique used for the switching signals generating of three level four leg Neutral Point Clamped (NPC) inverters controller.

Several strategies for switching signals generating to an multi-level four leg Neutral Point Clamped (NPC) SAPF with have been shown in the literature, such as the generation of switching signals by hysteresis [16,17], and by PWM [17, 18]. In this study, we use a new strategy called three level three Dimensional space vector modulation in the  $\alpha\beta0$ -axes (Three level 3D-SVM). Three level 3D-SVM ensures precise control with reduced harmonic distortion and constant the switching frequency compared to those obtained by hysteresis and PWM. Also this strategy not only inherits the fixation of switching frequency of inverter switches, but also improves the output voltage forms and provides a good dynamic response in the three level four leg inverter.

In this paper, to validate the correctness of the proposed new three level 3D-SVM strategy used for controlling the three level four leg Neutral Point Clamped (NPC) SAPF, the simulation of SAPF described previously was effected using Sim Power Systems and S-Function of MATLAB/SIMULINK. The objective of simulation is to study two different aspects: 1) The considerable decrease in shunt active power filter evaluation in comparison with Twolevels four leg SAPF controlled by two level 3D-SVM strategy proposed in [7] due to Three level four leg SAPF controlled by new three-level 3D-SVM strategy. 2) The reducing of output voltage harmonics, compensation of harmonics and reactive power, zero sequence current eliminating and switching frequency reducing under loads variations.

## II. MODELING OF THE THREE LEVEL FOUR LEG SHUNT ACTIVE POWER FILTER

The three level four leg shunt active power filter topology presented in this paper is shown in Fig. 1.

The main circuit contains a three phase non-linear load composed of three single phase Rectifier Bridge followed by  $R_{ch}$  and  $L_{ch}$  load, connected to a three phase source in a point called Point of Common Coupling (PCC).



Fig. 1. Three level four leg shunt active power filter topology

#### A. Three level four leg inverter modulation

As in the two level four leg inverter [20], each switch of three level four leg inverter  $T_{ij}$ ,  $i, j \in \{1, 2, 3, 4\}$  operates two by two complementary more precisely by the switching function as follows:

$$F_{j} = \begin{cases} 1 \text{ if } T_{1j} \text{ and } T_{2j} \text{ is closeds} \\ 0 \text{ if } T_{2j} \text{ and } T_{3j} \text{ is closeds} \\ -1 \text{ if } T_{3j} \text{ and } T_{4j} \text{ is closeds} \end{cases}$$
(1)

The operation two by two complementary switches is the following:

$$F_{ij} = 1 - F_{(i-2)j}, \ i = 3,4 \ ; \ j = 1,2,3,4$$
(2)

The three states of each leg  $F_j$  corresponding to the three switching functions  $F_{ij}$  is defined in the next way

$$F_{j} = \begin{cases} P \ if \ F_{ij} = 1 \\ O \ if \ F_{ij} = 0 \\ N \ if \ F_{ij} = -1 \end{cases}$$
(3)

The three level four leg inverter Fig. 4 delivers at the output three level voltages, these voltages are expressed in terms of the DC bus capacitors voltages  $V_{dc}/2$ , 0, and  $-V_{dc}/2$ , and according to three possible states **PON** switches of each leg [12, 13] as follows:

**State P**: The upper two switches  $T_{1j}$  and  $T_{2j}$  are closed, while the two lower switches  $T_{3j}$  and  $T_{4j}$  are open. The output voltage is  $v_i = \frac{V_{dc}}{2}$  **State O**: The middle two switches  $T_{2j}$  and  $T_{3j}$  are closed, while the two switches of the extremities  $T_{3j}$  and  $T_{4j}$  are open. The output voltage is.  $v_j = 0$ 

**State N**: The lower two switches  $T_{3j}$  and  $T_{4j}$  are closed, while the two upper switches  $T_{1j}$  and  $T_{2j}$  are open. The output voltage is  $v_j = \frac{-V_{dc}}{2}$ 

The output voltages are expressed by: [12, 13], [15], [21]

$$v_{jo} = F_j \cdot \frac{V_{dc}}{2} \tag{4}$$

TABLE I. STATES OF ONLY LEG OF INVERTER

States	Stat	tes of <i>i</i> swi	Output voltage		
$F_j$ of the leg $j$	$T_{lj}$	$T_{2j}$	$T_{3j}$	$T_{4j}$	v <sub>jo</sub>
Р	1	1	0	0	$\frac{V_{dc}}{2}$
0	0	1	1	0	0
N	0	0	1	1	$-V_{dc}/2$

 $v_{jo}$  is the output voltage of each leg. The output phase to neutral voltage is defined as:

$$v_{jn} = v_{jo} - v_{no} \tag{5}$$

Where  $v_{jo}$  is the voltage of the phase-middle imaginary point o,  $V_{dc}$  is the total DC bus voltage. Each leg of inverter can take three states (PON). Thus the three level four leg inverter is 3<sup>4</sup>=81 possible states. Table 2 summarizes the states of three level four leg inverter for each switching vector:

 
 TABLE II.
 The states of three level four legs inverter for Each switching vector

Vi	States	<i>v</i> <sub>i</sub>	States	<i>v</i> <sub>i</sub>	States
$v_I$	NNNN	V28	ONNN	V55	PNNN
<i>v</i> <sub>2</sub>	NNNO	V29	ONNO	V 56	PNNO
<i>V</i> 3	NNNP	V30	ONNP	V57	PNNP
$v_4$	NNON	V31	ONON	V 58	PNON
V5	NNOO	V32	ONOO	V 59	PNOO
$v_6$	NNOP	V33	ONOP	$v_{60}$	PNOP
V7	NNPN	V34	ONPN	V61	PNPN
$v_8$	NNPO	V35	ONPO	V <sub>62</sub>	POPO
V9	NNPP	V36	ONPP	<i>v</i> <sub>63</sub>	PNPP
<i>v</i> <sub>10</sub>	NONN	V37	OONN	$v_{64}$	PONN
<i>v</i> <sub>11</sub>	NONO	V38	OONO	V <sub>65</sub>	PONO
V12	NONP	V39	OONP	V66	PONP
<i>v</i> <sub>13</sub>	NOON	$v_{40}$	OOON	$v_{67}$	POON
V14	NOOO	V41	0000	V68	POOO
V15	NOOP	V42	OOOP	V69	POOP
V16	NOPN	V43	OOPN	V70	POPN
V17	NOPO	V44	OOPO	V71	POPO
<i>v</i> <sub>18</sub>	NOPP	V45	OOPP	V <sub>72</sub>	POPN
V19	NPNN	V46	OPNN	V73	PPON
V20	NPNO	V47	OPNO	V74	PPNO
<i>v</i> <sub>21</sub>	NPNP	V48	OPNP	V75	PPNP
<i>v</i> <sub>22</sub>	NPON	V49	OPON	V76	PPON
V23	NPOO	V50	OPOO	V77	PPOO
V24	NPOP	V51	OPOP	V <sub>78</sub>	PPOP
V25	NPPN	V52	OPPN	V79	PPPN
V26	NPPO	V <sub>53</sub>	OPPO	$v_{80}$	PPPO
V27	NPPP	V54	OPPP	V81	PPPP

The differential equations describing the dynamic model of four-leg shunt active power filter in the  $\alpha\beta0$ -axes are defined, as given in equation (6): [7], [20]

$$\frac{di_{f\alpha}}{dt} = -\frac{R_{f}}{L_{f}}i_{f\alpha} + \frac{1}{L_{f}}v_{f\alpha} - \frac{1}{L_{f}}v_{i\alpha} 
\frac{di_{f\beta}}{dt} = -\frac{R_{f}}{L_{f}}i_{f\beta} + \frac{1}{L_{f}}v_{f\beta} - \frac{1}{L_{f}}v_{i\beta} 
\frac{di_{f0}}{dt} = -\frac{R_{f}}{L_{f}}i_{f0} + \frac{1}{L_{f}}v_{f0} - \frac{1}{L_{f}}v_{i0} 
\frac{dV_{dc}}{dt} = \frac{P_{dc}^{*}}{CV_{dc}}$$
(6)

## III. THREE LEVEL THREE DIMENSIONAL SPACE VECTOR MODULATIONS

In 3D-SVM strategy in the three level four leg inverter, there are  $3^4$ =81 possible switching vectors: 79 active vectors and 3 null vectors. The Vector diagram of the three level four leg inverter is illustrated in Fig. 2.



Fig. 2. The three level four leg inverter diagram vector

#### A. Prisms and sub-prisms identification

Such as the vector diagram of two level four leg inverter [1-2], [5], the vector diagram of three level four leg inverter is composed of six prisms Fig. 5 are labeled Prisms I through VI, each prism is decomposed into four sub-prism Fig. 5 are labeled  $SP_1$ - $SP_4$  and each sub-prism is decomposed into *n* tetrahedrons Fig. 5-7 and are summarized in Table 2.

To detect which sub-prism is the reference vector, it is necessary to determine the equation that defines the three sides of each sub-prism  $(v_{f\alpha}^*, v_{f\beta}^*, v_{f0}^*)$  coordinates in  $\alpha\beta0$ -axes. In this case, and to minimize the harmonics of the output voltage [13], is imposed on the voltage of the reference vector that locate inside the hexagon delimited by the outer circle Fig.5, which gives:

$$v_{loc} = \frac{\sqrt{3}}{2} V_{dc} \tag{7}$$

The four sub-prisms of each prism are deduced by using the equations of eight straight delimited  $(d_1, d_2, ..., d_8 \text{ Fig. 6})$  that given as follows. [12]

$$\begin{pmatrix}
d_{1} : v_{f\beta}^{*} = -\sqrt{3}v_{f\alpha}^{*} + \sqrt{\frac{1}{2}}V_{dc} \\
d_{2} : v_{f\beta}^{*} = \sqrt{\frac{1}{8}}V_{dc} \\
d_{3} : v_{f\beta}^{*} = \sqrt{3}v_{f\alpha}^{*} - \sqrt{\frac{1}{2}}V_{dc} \\
d_{4} : v_{f\beta}^{*} = \sqrt{3}v_{f\alpha}^{*} + \sqrt{\frac{1}{2}}V_{dc} \\
d_{5} : v_{f\beta}^{*} = \sqrt{3}v_{f\alpha}^{*} + \sqrt{\frac{1}{2}}V_{dc} \\
d_{6} : v_{f\beta}^{*} = -\sqrt{3}v_{f\alpha}^{*} - \sqrt{\frac{1}{2}}V_{dc} \\
d_{7} : v_{f\beta}^{*} = -\sqrt{3}v_{f\alpha}^{*} - \sqrt{\frac{1}{2}}V_{dc} \\
d_{8} : v_{f\beta}^{*} = -\sqrt{\frac{1}{8}}V_{dc} \\
\begin{pmatrix}
d_{4} : v_{f\beta}^{*} = -\sqrt{\frac{1}{8}}V_{dc} \\
\end{pmatrix} \\
\begin{pmatrix}
d_{6} : v_{f\beta}^{*} = -\sqrt{\frac{1}{8}}V_{dc} \\
\end{pmatrix} \\
\begin{pmatrix}
d_{7} : v_{f\beta}^{*} = -\sqrt{\frac{1}{8}}V_{dc} \\
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\begin{pmatrix}
d_{7} : v_{f\beta}^{*} = -\sqrt{\frac{1}{8}}V_{dc} \\
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d_{7} : v_{f\beta}^{*} = -\sqrt{\frac{1}{8}}V_{dc} \\
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d_{7} : v_{f\beta}^{*} = -\sqrt{\frac{1}{8}}V_{dc} \\
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d_{7} : v_{f\beta}^{*} = -\sqrt{\frac{1}{8}}V_{dc} \\
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\begin{pmatrix}
d_{7} : v_{f\beta}^{*} = -\sqrt{\frac{1}{8}}V_{dc} \\
\end{pmatrix} \\
\end{pmatrix}$$

$$(d_{7} : v_{f\beta}^{*} = -\sqrt{\frac{1}{8}}V_{dc} \\
\end{pmatrix}$$



Fig. 3. Representation straight bounded sub-prism vector diagram of the three level four legs inverter.





Fig. 4. Representation of sub-prisms in the vector diagram of three level four leg inverter

Р	SP	
1	SP <sub>1-1</sub>	$v_{79}, v_{76}, v_{67}, v_{40}, v_{80}, v_{77}, v_{68}, v_1, v_{78}, v_{69}, v_2, v_{39}, v_{30}, v_3$
	SP <sub>2-1</sub>	v <sub>67</sub> , v <sub>64</sub> , v <sub>55</sub> , v <sub>68</sub> , v <sub>65</sub> , v <sub>56</sub> , v <sub>69</sub> , v <sub>66</sub> , v <sub>57</sub> , v <sub>30</sub>
	SP <sub>3-1</sub>	<i>v</i> <sub>76</sub> , <i>v</i> <sub>67</sub> , <i>v</i> <sub>64</sub> , <i>v</i> <sub>77</sub> , <i>v</i> <sub>68</sub> , <i>v</i> <sub>65</sub> , <i>v</i> <sub>78</sub> , <i>v</i> <sub>69</sub> , <i>v</i> <sub>66</sub> , <i>v</i> <sub>39</sub> , <i>v</i> <sub>30</sub>
	SP <sub>4-1</sub>	<i>v</i> <sub>76</sub> , <i>v</i> <sub>73</sub> , <i>v</i> <sub>64</sub> , <i>v</i> <sub>77</sub> , <i>v</i> <sub>74</sub> , <i>v</i> <sub>65</sub> , <i>v</i> <sub>78</sub> , <i>v</i> <sub>75</sub> , <i>v</i> <sub>66</sub> , <i>v</i> <sub>39</sub>
2	SP <sub>1-2</sub>	<i>v</i> <sub>79</sub> , <i>v</i> <sub>76</sub> , <i>v</i> <sub>49</sub> , <i>v</i> <sub>40</sub> , <i>v</i> <sub>77</sub> , <i>v</i> <sub>10</sub> , <i>v</i> <sub>1</sub> , <i>v</i> <sub>78</sub> , <i>v</i> <sub>11</sub> , <i>v</i> <sub>2</sub> , <i>v</i> <sub>39</sub> , <i>v</i> <sub>12</sub> , <i>v</i> <sub>3</sub>
	SP <sub>2-2</sub>	<i>v</i> <sub>76</sub> , <i>v</i> <sub>73</sub> , <i>v</i> <sub>46</sub> , <i>v</i> <sub>77</sub> , <i>v</i> <sub>74</sub> , <i>v</i> <sub>47</sub> , <i>v</i> <sub>78</sub> , <i>v</i> <sub>75</sub> , <i>v</i> <sub>48</sub> , <i>v</i> <sub>39</sub>
	SP <sub>3-2</sub>	$v_{76}, v_{49}, v_{46}, v_{77}, v_{10}, v_{47}, v_{78}, v_{11}, v_{48}, v_{39}, v_{12}$
	SP <sub>4-2</sub>	<i>v</i> <sub>49</sub> , <i>v</i> <sub>46</sub> , <i>v</i> <sub>19</sub> , <i>v</i> <sub>10</sub> , <i>v</i> <sub>47</sub> , <i>v</i> <sub>20</sub> , <i>v</i> <sub>11</sub> , <i>v</i> <sub>48</sub> , <i>v</i> <sub>21</sub> , <i>v</i> <sub>12</sub>
3	SP <sub>1-3</sub>	<i>v</i> <sub>79</sub> , <i>v</i> <sub>52</sub> , <i>v</i> <sub>49</sub> , <i>v</i> <sub>40</sub> , <i>v</i> <sub>53</sub> , <i>v</i> <sub>10</sub> , <i>v</i> <sub>1</sub> , <i>v</i> <sub>54</sub> , <i>v</i> <sub>11</sub> , <i>v</i> <sub>2</sub> , <i>v</i> <sub>15</sub> , <i>v</i> <sub>12</sub> , <i>v</i> <sub>3</sub>
	SP <sub>2-3</sub>	$v_{49}, v_{22}, v_{19}, v_{10}, v_{23}, v_{20}, v_{11}, v_{24}, v_{21}, v_{12}$
	SP <sub>3-3</sub>	$v_{52}, v_{49}, v_{22}, v_{53}, v_{10}, v_{23}, v_{54}, v_{11}, v_{24}, v_{15}, v_{12}$
	SP <sub>4-3</sub>	v <sub>52</sub> , v <sub>25</sub> , v <sub>22</sub> , v <sub>53</sub> , v <sub>26</sub> , v <sub>23</sub> , v <sub>54</sub> , v <sub>27</sub> , v <sub>24</sub> , v <sub>15</sub>
4	SP <sub>1-4</sub>	<i>v</i> <sub>79</sub> , <i>v</i> <sub>52</sub> , <i>v</i> <sub>43</sub> , <i>v</i> <sub>40</sub> , <i>v</i> <sub>53</sub> , <i>v</i> <sub>44</sub> , <i>v</i> <sub>1</sub> , <i>v</i> <sub>54</sub> , <i>v</i> <sub>45</sub> , <i>v</i> <sub>2</sub> , <i>v</i> <sub>15</sub> , <i>v</i> <sub>6</sub> , <i>v</i> <sub>3</sub>
	SP <sub>2-4</sub>	<i>v</i> <sub>52</sub> , <i>v</i> <sub>25</sub> , <i>v</i> <sub>16</sub> , <i>v</i> <sub>53</sub> , <i>v</i> <sub>26</sub> , <i>v</i> <sub>17</sub> , <i>v</i> <sub>54</sub> , <i>v</i> <sub>27</sub> , <i>v</i> <sub>18</sub> , <i>v</i> <sub>15</sub>
	SP <sub>3-4</sub>	v <sub>52</sub> , v <sub>43</sub> , v <sub>16</sub> , v <sub>53</sub> , v <sub>44</sub> , v <sub>17</sub> , v <sub>54</sub> , v <sub>45</sub> , v <sub>18</sub> , v <sub>15</sub> , v <sub>6</sub>
	SP <sub>4-4</sub>	<i>v</i> <sub>43</sub> , <i>v</i> <sub>16</sub> , <i>v</i> <sub>7</sub> , <i>v</i> <sub>44</sub> , <i>v</i> <sub>17</sub> , <i>v</i> <sub>8</sub> , <i>v</i> <sub>45</sub> , <i>v</i> <sub>18</sub> , <i>v</i> <sub>9</sub> , <i>v</i> <sub>6</sub>
5	SP <sub>1-5</sub>	<i>v</i> <sub>79</sub> , <i>v</i> <sub>70</sub> , <i>v</i> <sub>43</sub> , <i>v</i> <sub>40</sub> , <i>v</i> <sub>71</sub> , <i>v</i> <sub>44</sub> , <i>v</i> <sub>1</sub> , <i>v</i> <sub>72</sub> , <i>v</i> <sub>45</sub> , <i>v</i> <sub>2</sub> , <i>v</i> <sub>33</sub> , <i>v</i> <sub>6</sub> , <i>v</i> <sub>3</sub>
	SP <sub>2-5</sub>	<i>v</i> <sub>43</sub> , <i>v</i> <sub>34</sub> , <i>v</i> <sub>71</sub> , <i>v</i> <sub>44</sub> , <i>v</i> <sub>35</sub> , <i>v</i> <sub>8</sub> , <i>v</i> <sub>45</sub> , <i>v</i> <sub>36</sub> , <i>v</i> <sub>9</sub> , <i>v</i> <sub>6</sub>
	SP <sub>3-5</sub>	v <sub>70</sub> , v <sub>43</sub> , v <sub>34</sub> , v <sub>71</sub> , v <sub>44</sub> , v <sub>35</sub> , v <sub>72</sub> , v <sub>45</sub> , v <sub>36</sub> , v <sub>33</sub> , v <sub>6</sub>
	SP <sub>4-5</sub>	$v_{70}, v_{61}, v_{34}, v_{71}, v_{62}, v_{35}, v_{72}, v_{63}, v_{36}, v_{33}$
6	SP <sub>1-6</sub>	<i>v</i> <sub>79</sub> , <i>v</i> <sub>70</sub> , <i>v</i> <sub>67</sub> , <i>v</i> <sub>40</sub> , <i>v</i> <sub>71</sub> , <i>v</i> <sub>68</sub> , <i>v</i> <sub>1</sub> , <i>v</i> <sub>72</sub> , <i>v</i> <sub>69</sub> , <i>v</i> <sub>2</sub> , <i>v</i> <sub>33</sub> , <i>v</i> <sub>30</sub> , <i>v</i> <sub>3</sub>
	SP <sub>2-6</sub>	<i>v</i> <sub>70</sub> , <i>v</i> <sub>61</sub> , <i>v</i> <sub>58</sub> , <i>v</i> <sub>71</sub> , <i>v</i> <sub>62</sub> , <i>v</i> <sub>59</sub> , <i>v</i> <sub>72</sub> , <i>v</i> <sub>63</sub> , <i>v</i> <sub>60</sub> , <i>v</i> <sub>33</sub>
	SP <sub>3-6</sub>	<i>v</i> <sub>70</sub> , <i>v</i> <sub>67</sub> , <i>v</i> <sub>58</sub> , <i>v</i> <sub>71</sub> , <i>v</i> <sub>68</sub> , <i>v</i> <sub>59</sub> , <i>v</i> <sub>72</sub> , <i>v</i> <sub>69</sub> , <i>v</i> <sub>60</sub> , <i>v</i> <sub>33</sub> , <i>v</i> <sub>30</sub>
	SP <sub>4-6</sub>	$v_{67}, v_{58}, v_{55}, v_{68}, v_{59}, v_{56}, v_{69}, v_{60}, v_{57}, v_{30}$

THE THREE LEVEL FOUR LEG INVERTER SWITCHING TABLE III. VECTORS FOR EACH SUB-PRISM

#### B. Tetrahedrons identification

The tetrahedron is formed by four switching vectors, as shown in Fig. 8, these figure describes the representation of tetrahedron 1 plans belonging to first sub-prism SP<sub>1-1</sub>. [12]

For detecting at which tetrahedron is the reference vector  $\vec{v}_{f}^{*}$ , it is necessary to determine the equation defined the position of each tetrahedron in  $\alpha\beta0$ -axes. The first subprism of first prism is formed by ten tetrahedrons. For first sub-prism of first prism the tetrahedron  $T_1$  is combines by four switching vectors  $\{v_{79}, v_{76}, v_{67}, v_{40}\}$ , obeyed at the following position equation:

$$\begin{vmatrix} a.0+b.0+c = \frac{3}{2\sqrt{3}}V_{dc} \to v_{40} \\ a.\frac{V_{dc}}{\sqrt{6}}+b.0+c = \frac{2}{\sqrt{3}}V_{dc} \to v_{67} \\ a\frac{V_{dc}}{\sqrt{24}}+b\frac{\sqrt{2}}{4}V_{dc}+c = \frac{5}{2\sqrt{3}}V_{dc} \to v_{76} \end{cases}$$
(9)  
This gives:

$$a = \frac{\sqrt{2}}{2}, b = \sqrt{\frac{3}{2}}, c = \frac{3}{2\sqrt{3}}V_{dc}$$
(10)

The equation for detecting the position of first tetrahedron of first sub-prism of first prism is given by:

$$v_{fo}^* > \frac{\sqrt{2}}{2} v_{f\alpha}^* + \sqrt{\frac{3}{2}} v_{f\beta}^* + \frac{3}{2\sqrt{3}} V_{dc}$$
(11)

Fig.7 describes the representation of equation that detected the position of the first tetrahedron in first sub-prism of the first prism  $(SP_{1-1}-T_1)$ : The table 6 summarizes the four switching vectors of each tetrahedron for each sub-prism.



Fig. 5. Representation the position of first tetrahedron in the first sub-prism in the first prism (T1: SP1-1)

After that, the distributions of tetrahedrons in each subprism are shows in fig.6 and are given as follows:

- The sub-prism SP<sub>1</sub> content 10 tetrahedrons
- The sub-prism SP<sub>2</sub> content 8 tetrahedrons
- The sub-prisms SP<sub>3</sub> and SP<sub>4</sub> content 7 tetrahedrons



Fig. 6. Representation the distribution of tetrahedrons in each sub-prism

#### C. The time duration of the selected switching vectors

The principle of three level 3D-SVM is to project the desired switching vector on  $\alpha\beta0$ -axes, as shown in Fig. 5. We use these projections to calculate the switching time [7].

# D. The Switching controls generation

The Fig. 6 shows the distribution of switching vectors to be applied in the  $T_1$ :SP<sub>1-1</sub> on a switching period.



Fig. 7. Principle of switching signals generating by three level 3D-SVM

# IV. SIMULATION CONTROL OF THE FOUR LEG SHUNT ACTIVE POWER FILTRE

The work objective is to compare study of two different inverter topologies and their switches control uses in four leg SAPF. The inverter topologies and their switching signals generating that are considered for comparative study are: Two level four leg SAPF controlled by two level 3D-SVM proposed in [7] due to three level four leg SAPF controlled by new three level 3D-SVM. This is carried out by numerical simulation under the same conditions. The performance of the proposed control strategy is evaluated through Sim Power Systems and S-Function of MATLAB fig. 8.

The simulation results of the two topologies of four leg SAPF are given in Figs. (9-16), with the operating conditions: The DC voltage at the input of inverter is 800V, divided into two equal values, with two capacitors of  $5*10^{-3}$  Farads for each, and the sampling time *Te* is equal 100  $\mu$ s.

Figs 9 and 11 (a, b and c) represent the phase-to-neutral point output voltage  $v_{fln}$  and their analysis harmonics for the two topologies of four leg SAPF with the two types of switching signals generating (two level 3D-SVM and three level 3D-SVM) and with various values of Switching frequency (7, 10 and 14KHz), these figs shows that for same sampling time, the output voltage distortion harmonics THD are proportional with the Switching frequency.



Fig. 8. Schematic block diagram of a control of three level four leg shunt active power filter

The distortion harmonics of output voltages for both fourleg shunt active power filter are approximately centered around the multiples of report N between the period of commutation Ts and the period of output voltage T=0.02s.

For the case of  $f_s=7$  kHz,  $T_s=1/7000s$  and N=0.02\*7000 thus N=140 period, figs 9 and 11-a.

For the case of  $f_s=10 \ kHz$ ,  $T_s=1/10000s$  and N=0.02\*10000 thus N=200 period, figs 9 and 11-b.

For the case of  $f_s=14$  kHz,  $T_s=1/14000s$  and N=0.02\*14000 thus N=280 period, figs 9 and 11-c.

According to output voltages harmonics distortion (THDv) obtained for both four-leg shunt active power filter with the two types of switching signals generating under same switching frequency, it can be found that the output voltages harmonics distortion for same switching frequency are minimum in three level four leg SAPF controlled by three level 3D SVM as compared to two level four leg SAPF controlled by two level 3D SVM. This three level four leg SAPF controlled by three level 3D SVM also presents high output voltage forms.

Figs 11 and 12 shows the switching signals of the two topologies of four-leg shunt active power filter (impulses of first switch of first leg) for various values of switching frequency. These figures show that, for same conductions of simulations, even sampling period, and the same values of switching frequency, the switching losses are arrangement reduced in the three level four leg shunt active power filter controlled by three level SVM 3D (figs 11) compared to two level four leg shunt active power filter controlled by SVM 3D (Figs 12) [7].



Fig.12 Switching pulses of first switch (T1) of three level four leg SAPF controlled by three level 3D SVM

Figs. 13 and 14 (a, b and c) demonstrate the four feg shunt active power filter performance with the two topologies of four leg SAPF and their two types of switching signals generating under different loads conditions, the source currents waveform are sinusoidal and the neutral wire current is successfully reduced for all cases and various values of switching frequency, as well as smaller magnitudes than in the three level four leg SAPF controlled by three level 3D SVM. For both four leg SAPF with the two types of switching signals generating, the reactive power in the source is almost zero, which means also that the source has a power factor almost of unity before and after unbalanced loads, as well as smaller undulations than in the three level four leg SAPF controlled by three level 3D SVM.

The first phase source current spectra before and after unbalanced loads with various values of Switching frequency are given in Fig.15 and 16 (a, b and c) for both two level four leg SAPF controlled by two level 3D SVM [7] and three level four leg SAPF controlled by three level 3D SVM schemes are well below; the limit imposed by the IEEE-519 or CEI 61000 standards, and the total harmonics distortion for all various values and in same values of switching frequency are more lowest in the three level four leg SAPF controlled by three level 3D SVM compared to the two level four leg SAPF controlled by 3D SVM [7].



Fig. 16 Spectrum of source current for three level four leg SAPF controlled by three level 3D SVM: (i) before unbalanced loads, (ii) after unbalanced loads

## V. CONCLUSION

In this work theoretical study and verify with simulation of a shunt active power filter with three level four ,leg inverter NPC structure is proposed to improve the power quality under unbalanced loads. And a new three level Three Dimensional Space Vector Modulation (Three level 3D-SVM) control strategy was presented for switching signals generating of the three level four leg inverter. This control strategy accomplished to reduce the switching losses, fixed switching frequency and to improve the inverter output voltages forms over the conventional control strategies. The simulation results of three level four leg SAPF controlled by three level 3D SVM also shows better dynamic performances over the two level four leg SAPF controlled by 3D SVM. The following objectives have been successfully carried even with three level four leg SAPF controlled by three level 3D SVM under unbalanced loads: 1) Harmonics and zero-sequence current filtering and minimizing.

2) Switching losses reducing, and fixed switching frequency of inverter switches.

3) Neutral wire current magnitude and reactive power undulations reducing's.

- 4) Reactive power compensation.
- 5) The inverter output voltages forms improved.

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